## **Structure and Magnetism of Neutral and Anionic Palladium Clusters**

M. Moseler, H. Häkkinen, R. N. Barnett, and Uzi Landman

School of Physics, Georgia Institute of Technology, Atlanta, Georgia 30332-0430

(Received 15 August 2000)

The properties of neutral and anionic  $Pd_N$  clusters were investigated with spin-density-functional calculations. The ground-state structures are three dimensional for N > 3 and they are magnetic with a spin triplet for  $2 \le N \le 7$  and a spin nonet for N = 13 neutral clusters. Structural and spin isomers were determined and an anomalous increase of the magnetic moment with temperature is predicted for a  $Pd_7$  ensemble. Vertical electron detachment and ionization energies were calculated and the former agrees well with measured values for  $Pd_N^-$ .

## DOI: 10.1103/PhysRevLett.86.2545

PACS numbers: 36.40.Cg, 36.40.Mr, 36.40.Wa, 61.46.+w

Enhancement of magnetism in clusters of elements that are ferromagnetic as bulk solids has been demonstrated through Stern-Gerlach (SG) deflection measurements [1], and it is understood to derive from reduced atomic coordination resulting in stronger electron localization. However, the emergence of magnetism in small clusters of close-shell nonmagnetic atoms is clouded by uncertainty. Palladium aggregates (with a [Kr]  $4d^{10}$  atomic structure) are particularly interesting since the bulk metal is known to be "almost" magnetic, with the emergence of magnetism predicted to require a mere 6% lattice expansion [2]. Experimental information is limited to SG measurements on  $Pd_N$  clusters with N > 12 (which were found to be nonmagnetic) [3] or to inferences from (nonmagnetic) photoemission studies [4]. Systematic theoretical investigations of magnetic properties are lacking, limited only to neutral Pd<sub>13</sub> [5,6].

We report on an extensive density-functional-theory study pertaining to size-dependent patterns of the properties of  $Pd_N$  and  $Pd_N^-$  clusters with N = 1-7 and N = 13. The ground states (GSs) of the neutral and anionic clusters are found to undergo an early transition (i.e., for N > 3) to three-dimensional (3D) ones and possess a nonzero magnetic moment. In addition to higher-energy structural isomers (STIs) we determined sequences of close-lying spin isomers (SPIs). For a Pd<sub>7</sub> ensemble, we predict an increase of the magnetic moment with temperature due to the thermal accessibility of such isomers. All the SPIs exhibit high local magnetic moments (LMMs), including the singlet states with an antiferromagnetic LMM coupling. Our structural determinations are corroborated by the remarkable agreement between the calculated vertical electron detachment energies (vDEs) from the cluster anions and photoelectron spectroscopy (PES) measurements [4,7,8].

In this study the Kohn-Sham (KS) equations with generalized gradient corrections [9] were solved using the Born-Oppenheimer local-spin-density molecular dynamics method [10], with scalar-relativistic [11] nonlocal pseudopotentials [12]. Cluster geometries were determined via symmetry-unrestricted structural optimizations through an exhaustive search among various structures including those suggested for certain Pd clusters [13–15] and other metal clusters [16,17]. For each structure spin-restricted optimizations were performed covering all energetically important spin multiplicities.

The GS geometries and STIs for both  $Pd_N$  and  $Pd_N^-$  are rather similar and they follow the same structural evolution, exhibiting Jahn-Teller distortions from the ideal symmetric structures (see Fig. 1), with a transition to 3D configurations at N > 3 [18]. The GSs (i.e., maximal binding energy  $E_B$  in Fig. 1) of Pd<sub>N</sub> with  $N \leq 7$  have a triplet (S = 1) spin multiplicity (see open squares in Figs. 1A–1F), while for  $Pd_{13}$  the GS is associated with a nonet (S = 4) spin configuration (see Fig. 1G). On the other hand, the GS spin multiplicities of the  $Pd_N^-$  anions (filled symbols in Fig. 1) vary nonmonotonically with N(doublet for N = 2, 3, 4, and 6; quartet for N = 5; sextet for N = 7, and octet for N = 13). We note here that the higher-lying STIs [19] and SPIs of the neutral and anionic clusters become thermally accessible with increasing cluster size (see temperature scales [20] on the right-hand side of Fig. 1).

The binding energies of the GS clusters increase rather monotonically with N (Fig. 2a), showing enhanced local stabilities for Pd<sub>3</sub><sup>-</sup> and Pd<sub>4</sub> [21]. The average nearest-neighbor bond lengths ( $\langle R_{nn} \rangle$ ) of the GS structures and the SPIs are very similar [22], converging rapidly to the bulk value (2.75 Å [23]).

The calculated vDEs from the cluster anions are in remarkable agreement with values determined from PES measurements [4,7,8] (Fig. 2b). For all the clusters, we display the vDEs only for the GS (structural and spin) configurations of the anions, except for  $Pd_7^-$  where we show the vDEs for both the GS (S = 5/2) and its next (higher-in-energy) SPI (S = 3/2) (the difference in energy between the two isomers is 0.11 eV, corresponding to only 170 K in vibrational temperature [20]), with the latter exhibiting a better agreement with the experimental data. These results suggest that for  $Pd_7^-$  the measured vDE may correspond to this higher-energy SPI which is accessible already at very low temperatures, while for the other clusters studied here the vDEs are determined by the GS structures over a broad temperature range. The only (slight) discrepancy between the calculated and measured vDEs is for  $Pd_3^-$  (see Fig. 2b). However, we observe from this figure that the predicted vDE (2.0 eV) for  $Pd_3^-$  is rather close to the dissociation energy ( $E_D$ ) of the process  $Pd_3^- \rightarrow Pd_2^- + Pd$  (see filled circle in Fig. 2b at  $E_D = 2.41$  eV, compared to a measured value of 2.26 eV [24]). This implies that this dissociation channel may compete with the electron detachment under appropriate ex-



perimental conditions. Consequently, we assign the vDE of  $Pd_3^-$  to the next higher feature in the measured PES [8]) occurring at 1.88 eV which agrees with the predicted value, and the lower measured value (at 1.66 eV, marked by a cross in Fig. 2b) is attributed to the vDE of a (hot)  $Pd_2^-$  dissociation product [25] (the same conclusions apply to the photoelectron spectrum of  $Pd_3^-$  shown in Fig. 2 of Ref. [4]); for a similar interpretation of the measured PES of  $Au_3^-$ , see Refs. [16] and [26].

The vertical ionization potentials predicted by us (vIP in Fig. 2c) start at the atomic value of 8.28 eV compared to the measured first IP of Pd, 8.33 eV [23]; the calculated second IP of Pd (27.34 eV) also agrees with the experimental one (27.75 eV) [23]. The predicted values for N = 2 and 3 are close to each other followed by a marked drop for clusters with N > 3, which is likely to reflect the transition to 3D structures. Convergence to the bulk limit (the work function of Pd is 4.97 eV [27]) is slow. No measured IP values have been reported.

The multitude of spin multiplicities for the  $Pd_N^-$  clusters results in a considerable variation of the magnetic moment per atom  $\mu = 2S \mu_B/N$  (solid squares in Fig. 2d) with particularly high values of  $\mu = 0.6, 0.71$ , and  $0.54 \mu_B$  for N = 5, 7, and 13, respectively. On the other hand, the occurrence of a triplet GS for the neutral clusters underlies a monotonic 1/N decrease of  $\mu$  for N = 1-7 (open squares in Fig. 2d), with an unexpected high value of  $0.62 \mu_B$  for  $Pd_{13}$  which is higher than the experimental [3] estimate ( $\mu < 0.4 \mu_B$ ).

The rather surprising existence of energetically favorable high-spin isomers for Pd clusters originates from *sd* hybridization developing upon bonding, with the *d*-orbitals' weight diminished somewhat on each atom, resulting in a situation reminiscent of open-shell transition metals. The total magnetic moment of the cluster is comprised of sizable atomic LMMs [ $\mu_{\ell} \sim \pm (0.3 - 0.6)\mu_B$ ] that couple antiferromagnetically in the spin-compensated

FIG. 1. Binding energies  $E_B$  (in eV) of structural (a, b, c) and spin (S = 0, 1/2, 1, 3/2, etc.) isomers of  $Pd_N^-$  and  $Pd_N$  for N = 1-7 (A)–(F) and 13 (G). Filled and open symbols represent anions and neutrals, respectively, and squares for the ground-state structure (a), circles for structures (b), and triangles for (c). The anionic  $E_B$  is defined as the energy per atom to separate  $Pd_N^{-}$  into N neutral atoms and an electron. The  $E_B$  values on the left-hand side of the panels are mapped on separate temperature scales [20] (T, in K) for the anions (top values on the right-hand axis of each panel) and the neutrals (bottom values), giving an estimate of the thermal accessibility of the isomers. Note the large number of isomers for Pd<sub>7</sub> and  $Pd_7^-$  for T < 400 K. Some of the structural isomers were not stable for certain spin values (such cases are denoted by dashed lines). The Pd<sub>4</sub><sup>-</sup> square (b) in panel (C) transformed into a rhombus (c) for S = 3/2 and the Pd<sub>4</sub> rhombus transformed into a square for S = 0 and 1. The Pd<sub>6</sub> capped trigonal bipyramid (b) transformed to the octahedron (a) for S = 0. The Pd<sub>7</sub> capped octahedron (b) became a pentagonal bipyramid (a) for S = 3 and the Pd<sub>13</sub> and Pd<sub>13</sub><sup>-</sup> cuboctahedron (b) transformed to the icosahedron (a) for S = 9/2 and 5, respectively.



FIG. 2 (color). Size evolution [panels (a)-(d)] of energetic and magnetic quantities in Pd clusters. (a) Binding energy per atom,  $E_B$  (in eV); (b) theoretical (filled squares) and experimental (open circles) vertical electron detachment energy (vDE) and the calculated atom dissociation energy  $E_D$  of the anions (filled circles). Experimental values are taken from Refs. [7,8] for N = 1-3 (the corresponding results shown for  $Pd_3^-$  in Fig. 2 of Ref. [4] are essentially the same) and from [4] for N = 4-7 and 13. The cross and the open circle at N = 3 correspond to the maximum of peak A and the peak of group B-H in Fig. 1 of Ref. [8], respectively (and correspondingly for the first and second peaks in Fig. 2 of Ref. [4]). For Pd7<sup>-</sup> we show the vDE of the GS (S = 5/2)and a thermally accessible SPI (S = 3/2). The vDE of  $Pd_1^-$  was estimated according to Janak's theorem [28] by the highest occupied molecular orbital energy of  $Pd_1^{-1/2}$ ; (c) calculated vertical ionization potentials; (d) the magnetic moment per atom of the GS anions (filled squares) and of the GS neutrals (open squares). (e),(f) Density of states (DOS, in 1/eV) of singlet (e) and nonet (f) icosahedral Pd<sub>13</sub> clusters. (g) Constant-value images of spin-polarization density in singlet, quintet, and nonet icosahedral Pd<sub>13</sub> (left, middle, right, respectively) clusters. The purple and yellow denote excess of minority and majority spins, respectively. Note the transition from antiferromagnetic to ferromagnetic ordering when going from the singlet to the nonet.

singlet states, and align themselves in SPIs with high total  $\mu$ . This is illustrated for the icosahedral Pd<sub>13</sub> cluster in Fig. 2 where the (gapless) density of states (DOS) of the S = 0 singlet SPI is shown in Fig. 2e and the corresponding spin-polarization density in Fig. 2g (left); note the nonuniform spatial distribution of the spin polarization reflected in the different line shapes of the DOS of the up and down spins. In the S = 2 spin-quintet SPI the minority spin polarization is localized on three sites located in a triangle (Fig. 2g, middle). In the S = 4spin-nonet GS cluster all the sites are spin polarized in the same direction (Fig. 2g, right), and its stability is reflected in the large gap in the majority-spin DOS near the Fermi energy (see spin  $\uparrow$  in Fig. 2f).

Intriguing conclusions can be made regarding the thermal behavior of certain Pd clusters in SG measurements; here we consider the case of Pd<sub>7</sub> and Pd<sub>7</sub><sup>-</sup> at room temperature. Neglecting the vibrational and entropic differences between the isomers, the probability to find a cluster with spin *S*, irrespective of its atomic isomeric structure, is given by  $P_{N,T}(S) = \sum_{I} \exp(\frac{NE_B(N,I,S)}{k_BT})/Z_{N,T}$ with the Boltzmann constant  $k_B$ , the ensemble temperature *T*, the structural isomer index *I*, and the (normalizing)

partition function  $Z_{N,T}$ . Several spin isomers of the neutral as well as the anionic heptamer have a finite  $P_{7,T}(S)$  (Fig. 3a) even for low temperatures, leading us to predict that in a SG experiment up to three different deflection angles should be measurable. Note that while an increase in temperature depopulates the Pd<sub>7</sub> pentagonal bipyramid triplet (S = 1) GS, the singlet (S = 0) state of that structure and the capped octahedron quintet (S = 2)state (Fig. 1F) gain statistical weight. Consequently, we predict that for Pd7 a rise in temperature would lead first to a decrease of the thermally averaged magnetic moment per atom  $\langle \mu \rangle_{N,T} = \sum_{S} 2S \mu_B P_{N,T}(S)/N$  due to a sharp increase in the population of the singlet state. The subsequent increase of  $\langle \mu \rangle_{NT}$  (see Fig. 3b, T > 200 K) results from the higher thermal population of the quintet state relative to the GS triplet (Fig. 3a) [29]. Such anomaly does not occur in the case of the Pd7<sup>-</sup> cluster where the doublet (S = 1/2) and quartet (S = 3/2) states start to coexist with the sextet (S = 5/2) GS at elevated temperatures (Fig. 3a). For both neutral and anionic  $Pd_{13}$ , the higher-lying isomers play essentially no role for T < 800 K resulting in a weak temperature dependence of  $\langle \mu \rangle_{N,T}$  (Fig. 3b).



FIG. 3. (a) Population probabilities of the different SPIs (irrespective of the structure) of neutral (dashed curves) and anionic (solid curves) heptamers; (b) thermally averaged magnetic moments per atom for  $Pd_7$ ,  $Pd_7^-$ ,  $Pd_{13}$ , and  $Pd_{13}^-$ .

In summary, we found that unlike atomic and bulk Pd, both neutral and anionic  $Pd_N$  clusters ( $2 \le N \le 7$  and N = 13) are magnetic, with relatively high LMMs. Underlying this behavior is the hybridization of atomic s and d states when clusters are formed that depletes local d contribution around each atom and leads to an open-shell-like behavior. The abundance of close-lying SPIs for certain clusters should be detectable in thermally controlled SG experiments, and we predict an ensemble of Pd<sub>7</sub> clusters to exhibit an (anomalous) increase of the magnetic moment with temperature. The remarkable agreement between the calculated and measured vDEs of the cluster anions corroborates the predicted atomic structures. Our results provide the first quantitative predictions pertaining to the emergence of pronounced magnetic properties of  $Pd_N$  and  $Pd_N^-$  clusters, unlike the weak magnetic tendencies inferred indirectly from PES data [4]; note, in particular, the contrast between our results for Pd<sub>7</sub> (see Fig. 2d and Fig. 3) and the suggestion of a zero spin GS for Pd<sub>7</sub> given in Ref. [4]. Furthermore, our study motivates temperature-dependent magnetic deflection (SG) measurements and further investigations of free and supported Pd clusters, including correlations between their magnetic properties and their catalytic activity [30].

This work is supported by the U.S. DOE, the Deutsche Forschungsgemeinschaft (M.M.), and the Academy of Finland (H.H.). Computations have been done on IBM SP2 at the Georgia Tech Center for Computational Materials Science and on Cray T3E at NERSC.

- [1] I. M. L. Billas et al., Science 265, 1692 (1994).
- [2] V.L. Moruzzi and P.M. Marcus, Phys. Rev. B **39**, 471 (1989).
- [3] A.J. Cox et al., Phys. Rev. B 49, 12295 (1994).
- [4] G. Ganteför and W. Eberhardt, Phys. Rev. Lett. 76, 4975 (1996).
- [5] B. V. Reddy et al., Phys. Rev. Lett. 70, 3323 (1993).
- [6] N. Watari and S. Ohnishi, Phys. Rev. B 58, 1665 (1998).
- [7] J. Ho et al., J. Phys. Chem. 95, 4845 (1991).
- [8] K. M. Ervin et al., J. Phys. Chem. 89, 4514 (1988).
- [9] J. P. Perdew et al., Phys. Rev. Lett. 77, 3865 (1996).
- [10] R. Barnett and U. Landman, Phys. Rev. B 48, 2081 (1993).
- [11] L. Kleinman, Phys. Rev. B 21, 2630 (1980); G. B. Bachelet and M. Schlüter, Phys. Rev. B 25, 2103 (1982).

- [12] N. Troullier and J.L. Martins, Phys. Rev. B **43**, 1993 (1991). The core radii (in units of  $a_0$ ) are s(2.45), p(2.6), and d(2.45) with s as the local component. A plane-wave basis with a 61.67 Ry cutoff was used.
- [13] D. Dai and K. Balasubramanian, Chem. Phys. Lett. 310, 303 (1999), and references therein.
- [14] G. Valerio and H. Toulhoat, J. Phys. Chem. 100, 10827 (1996).
- [15] K. M. Neyman et al., Appl. Catal. 191, 3 (2000).
- [16] H. Häkkinen and U. Landman, Phys. Rev. B 62, R2287 (2000).
- [17] V. Bonacic-Koutecky *et al.*, J. Chem. Phys. **98**, 7981 (1993).
- [18] The symmetries of the ideal structures are Pd<sub>3</sub>:  $D_{3h}$  equilateral triangle, Pd<sub>4</sub>:  $T_d$  tetrahedron, Pd<sub>5</sub>:  $D_{3h}$  trigonal bipyramid, Pd<sub>6</sub>:  $O_h$  octahedron, Pd<sub>7</sub>:  $D_{5h}$  pentagonal bipyramid, and Pd<sub>13</sub>:  $I_h$  icosahedron. Atomic coordinates of the neutral and anionic clusters are available upon request.
- [19] The ideal symmetries of the higher-energy STIs are Pd<sub>3</sub>:  $D_{\infty h}$  linear chain, Pd<sub>4</sub>:  $D_{4h}$  square and  $D_{2h}$  rhombus, Pd<sub>5</sub>:  $C_{4,\nu}$  tetragonal pyramid, Pd<sub>6</sub>:  $C_{2\nu}$  capped trigonal bipyramid, Pd<sub>7</sub>:  $C_{3\nu}$  capped octahedron,  $C_{3\nu}$  tricapped tetrahedron, and Pd<sub>13</sub>:  $O_h$  cuboctahedron.
- [20] The thermal accessibility of an N atom isomer is estimated by  $T = 2(NE_{B,GS} - NE_{B,isomer})/(3N - 6)k_B$ .
- [21] For both the neutral (0.69 eV/atom) and anionic (1.29 eV/atom) dimers the calculated binding energies overestimate somewhat the experimental values of  $0.52 \pm 0.08$  and  $1.08 \pm 0.09$  eV/atom (see Ref. [7]), respectively.
- [22]  $\langle R_{nn} \rangle$  values range from 2.53 Å (2.49 Å) for Pd<sub>2</sub> (Pd<sub>2</sub><sup>-</sup>) to 2.77 Å (2.78 Å) for Pd<sub>13</sub> (Pd<sub>13</sub><sup>-</sup>). The reduced bond length of the spin doublet GS of Pd<sub>2</sub><sup>-</sup> agrees with experiments (0.037 Å reduction) [8]. Inspection of the KS molecular orbitals (MO) of Pd<sub>2</sub> reveals that the highest occupied MO and the lowest unoccupied one (LUMO) are *both sd* hybridized *bonding* states of the same spatial symmetry but with different spins, and consequently formation of the dimer anion (involving occupation of the LUMO) strengthens the bond and shortens it.
- [23] C. Kittel, Introduction to Solid State Physics (Wiley, New York, 1996).
- [24] V. Spasov and K. Ervin, J. Chem. Phys. 109, 5344 (1998).
- [25] Indeed, the lowest measured [8] electron binding energy peak for  $Pd_3^-$  at 1.66 eV essentially coincides with the vDE determined from the PES of  $Pd_2^-$  [7] (see open circle for N = 2 in Fig. 2b). However, the measured PES peak at 1.66 eV does not exhibit a vibrational structure characteristic to a dimer [8].
- [26] J. Ho et al., J. Phys. Chem. 93, 6987 (1990).
- [27] CRC Handbook of Chemistry and Physics, edited by R.C. Weast (CRC Press, Cleveland, OH, 1974), 55th ed.
- [28] J.F. Janak, Phys. Rev. B 18, 7165 (1978).
- [29] Such an anomalous behavior was observed in SG experiments for large Fe clusters (Ref. [1]) and it has been attributed to a crystal phase transformation, in analogy with the expected coexistence at finite temperature of the  $D_{5h}$  and capped  $O_h$  structures found here for Pd<sub>7</sub>.
- [30] U. Heiz and W-D. Schneider, in *Metal Cluster at Surface*, edited by K. H. Meiwes-Broer (Springer, Berlin, 2000).